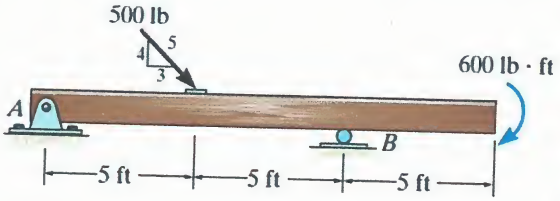
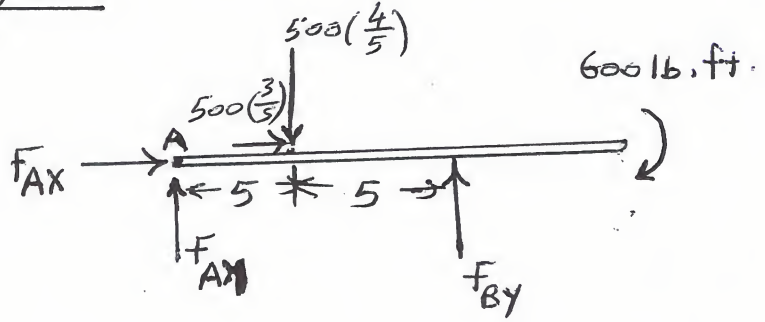
(1)

1 Determine the horizontal and vertical components of reaction at the supports. Neglect the thickness of the beam.

(Ans. $A_x = 300\ lb, A_y = 140\ lb, B_y = 260\ lb$)



* I- we draw a free body diagram.



$\xrightarrow{+} \Sigma F_X = 0$

$F_{AX} + 500\left(\frac{3}{5}\right) = 0$

$F_{AX} = -300\ lb$

F_{AX}

∴ ~~The resultant force in~~ X - direction = 300 lb in the negative x - direction.

$\overset{+}{\circlearrowleft} \Sigma M_A = 0$ ∴ $F_{By}(10) - 500\left(\frac{4}{5}\right)(5) - 600 = 0$

$10 F_{By} - 2000 - 600 = 0$

∴ $10 F_{By} = 2600$

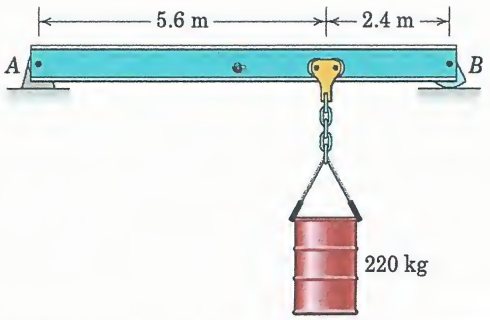
∴ $F_{By} = 260\ lb.$

∴ $F_{By} = 260\ lb$, its direction is in the +ve y direction.

$+\uparrow \Sigma F_y = 0$ ∴ $F_{Ay} - 500\left(\frac{4}{5}\right) + 260 = 0$

∴ $F_{Ay} = 400 - 260 = 140\ lb.$

2 Determine the reactions at the supports at A and B, and the tension in the cable. The I-beam is uniform with weight = 450 kg. (Ans. $A_x = 0\,N,\ A_y = 2850\,N, B_y = 3720N$)



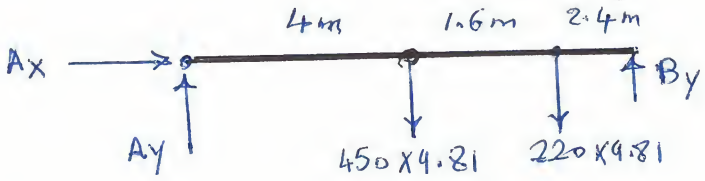
- Pin ~~Connect~~ support at A then we have A_x, A_y
- rocker support at B. then we have force ⊥ the surface at the point of contact.

$\xrightarrow{+} \Sigma F_x = 0$

$\therefore A_x = 0$

$+\uparrow \Sigma F_y = 0$

$B_y + A_y - (220 \times 9.81) - 450 \times 9.81 = 0$



$\therefore A_y + B_y = 6572.7 \quad -①$

$\overset{+}{\circlearrowleft} \Sigma M_A = 0$

$B_y(8) - (220 \times 9.81) \times 5.6 - (450 \times 9.81) \times 4 = 0$

$8B_y = 29743.92$

$\therefore \boxed{B_y = 3718\ N.}$

$\therefore A_y = 6572.7 - 3718$

$\boxed{A_y = 2854.7\ N.}$

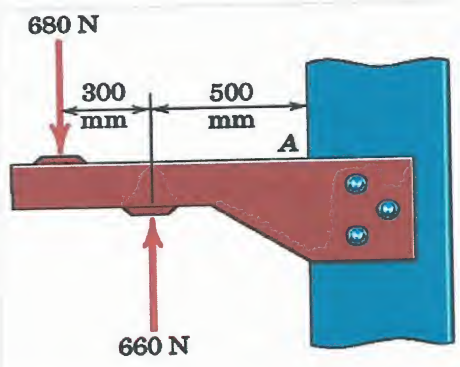
$\boxed{A_x = 0}$

Tension in the cable = ??

~~$220 \times 9.81 =$~~ $T = 220 \times 9.81 = 2158\ N.$

3 Determine the reactions at the support A.

(Ans. $A_x = 0N, A_y = 20\ N, M_A = -214\ N.m$)



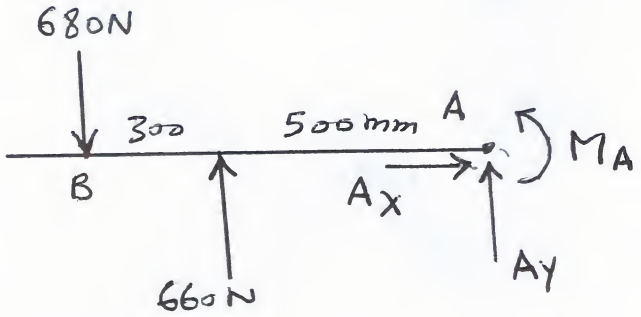
$\xrightarrow{+} \Sigma F_x = 0$

$A_x = 0\ N$

$+\uparrow \Sigma F_y = 0$

$A_y + 660 - 680 = 0$

$A_y = 680 - 660 = 20\ N$



$+\circlearrowleft \Sigma M_B = 0$

$660 \times 0.3M + A_y (0.8m) + M_A = 0$

$(660 \times 0.3) + 20(0.8) + M_A = 0$

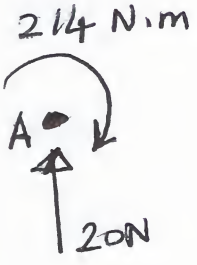
$\therefore M_A = -20(0.8) - 660(0.3)$

$M_A = -214\ N.m$

∴ At support A we have 2 reactions:

① Force = 20 N in the positive direction of Y.

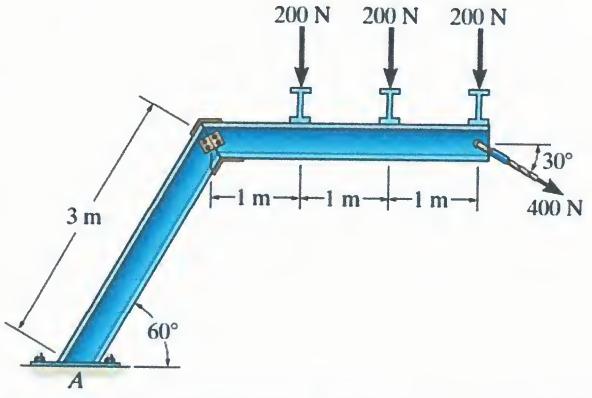
② Moment = 214 N.m in the C.W direction.



(4)

4 Determine the components of reaction at the fixed support A. Neglect the thickness of the beam.

(Ans. $A_x = 346\ N$, $A_y = 800\ N$, $M_A = 3900\ N.m$)

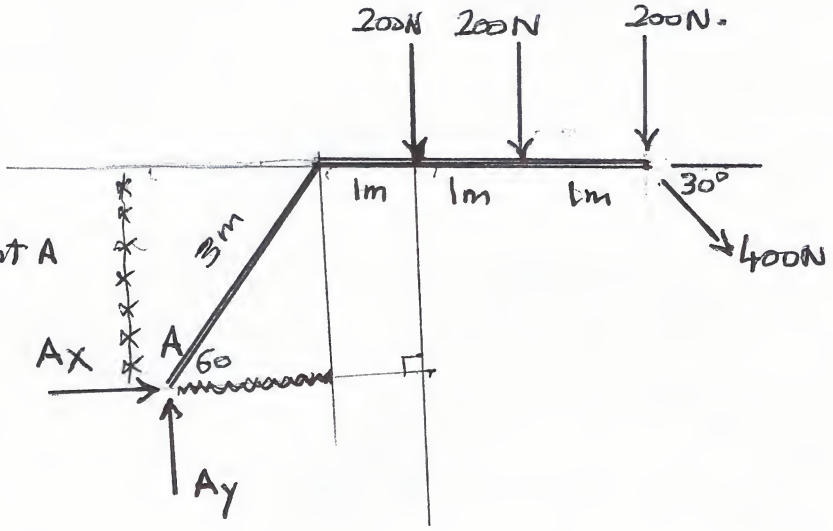


$\xrightarrow{+} \Sigma F_x = 0$

$A_x + 400 \cos 30 = 0$

$\therefore A_x = -346\ N.$

∴ the x-component at point A is equal to 346 N and acts in the -ve direction of x-axis.



$+\uparrow \Sigma F_y = 0$

$A_y - 200 - 200 - 200 - 400 \sin 30 = 0$

$A_y = 800\ N$

∴ The y-component at point A is equal to 800N and acts in the +ve direction of Y.

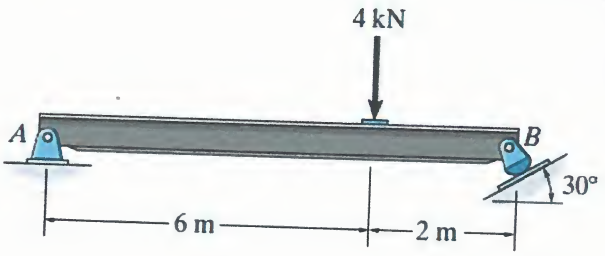
$\overset{+}{\circlearrowleft} M_A = -200(1 + 3\cos 60) - 200(2 + 3\cos 60) - 200(3 + 3\cos 60) - 400\cos 30\,(3\sin 60) - 400 \sin 30 (3 + 3\cos 60)$

$\overset{+}{\circlearrowleft} M_A = -500 - 700 - 900 - 900 - 900$

$M_A = -3900\ N.m$ ∴ $M_A = 3900\ N.m$ C.W around A.

(5)

5 Determine the horizontal and vertical components of reaction at the pin A and the reaction of the rocker B on the beam.



(Ans. $A_x = 1.73\ kN,\ A_y = 1\ kN,$ $N_B = 3.46\ kN$)

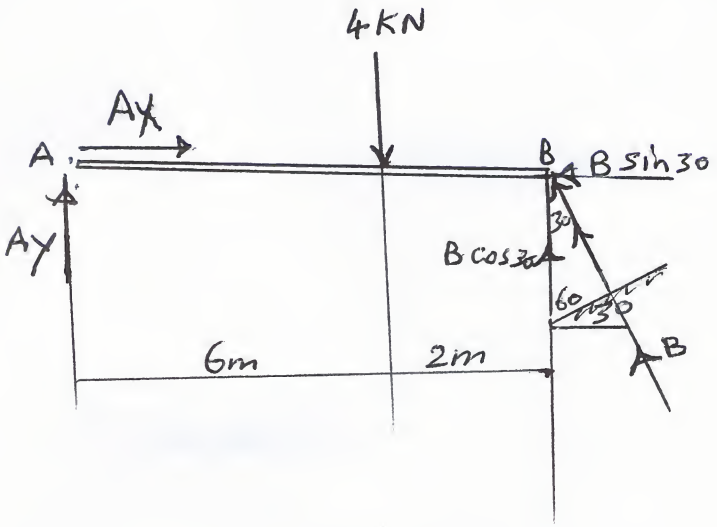
$\xrightarrow{+} \Sigma F_x = 0$

$A_x - B \sin 30 = 0$

$+\uparrow \Sigma F_y = 0$

$A_y - 4 + B \cos 30 = 0$

$+ \circlearrowleft \Sigma M_A = 0$



$B \cos 30\,(8) - 4\,(6) = 0$

$8B\,\frac{\sqrt{3}}{2} - 24 = 0 \;\Rightarrow\; \frac{8B\sqrt{3}}{2} = 24 \;\Rightarrow\; 4B\sqrt{3} = 24$

$\therefore B\sqrt{3} = 6 \;\therefore B = \frac{6}{\sqrt{3}} = \frac{6\sqrt{3}}{3} = 2\sqrt{3} = 3.46$ KN.

$A_x = B \sin 30$

$\therefore A_x = 3.46\left(\frac{1}{2}\right)$ KN.

$\boxed{A_x = 1.73\,KN}$

$A_y = 4 - B \cos 30$

$A_y = 4 - 2\sqrt{3}\left(\frac{\sqrt{3}}{2}\right) = 4 - 3 = 1$ KN.

$\boxed{A_y = 1\,KN}$

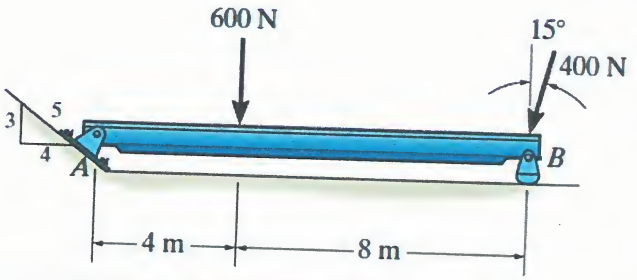
reaction of the rocker B on the Beam $= B = 3.46$

$\boxed{\text{reaction on B} = 3.46KN}$

(6)

6 Determine the magnitude of the reactions on the beam at A and B. Neglect the thickness of the beam.

(Ans. $B_y = 586\ N, F_A = 413\ N$)



$\xrightarrow{+} \Sigma F_x = 0$

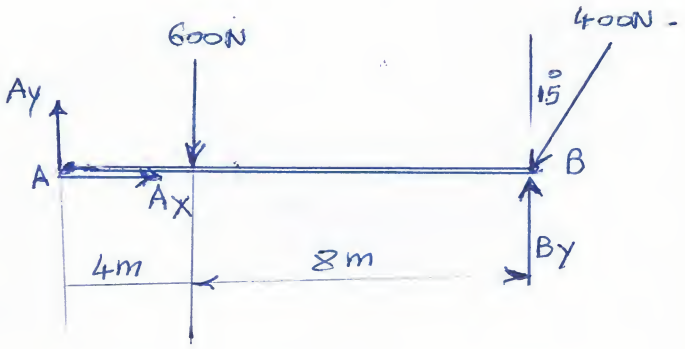
$A_x - 400 \sin 15 = 0$

$A_x = 103.528\ N$ — (1)

$\uparrow^{+} \Sigma F_y = 0$

$A_y + B_y - 600 - 400 \cos 15 = 0$

$A_y + B_y = 986.37\ N$ — (2)



$\circlearrowleft_{+} \Sigma M_A = 0$

$B_y(12) - (400 \cos 15)(12) - 600(4) = 0$ — (3)

From (3) get B_y

$12B_y = 7036.444$

$\therefore \boxed{B_y = 586\ N}$

From (3)

$\therefore A_y = 986.37 - 586 = 400.37\ N.$

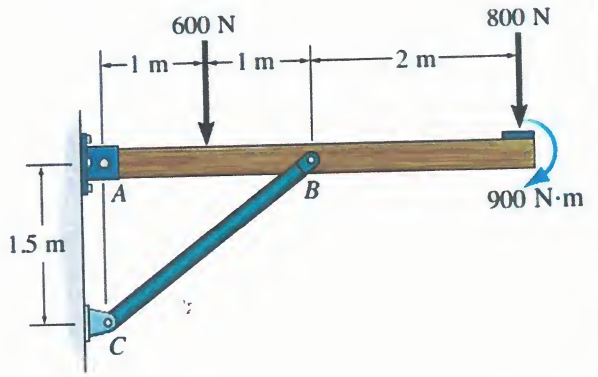
$\boxed{A_y = 400.37 N}$

$F_A = \sqrt{(103.528)^2 + (400.37)^2} = 413.54N$

$\boxed{F_A = 413.5 N}$

(7) 7 The overhanging beam is supported by a pin at A and the two-force strut BC. Determine the horizontal and vertical components of reaction at A and the reaction at B on the beam.

(Ans. $A_x = 3133.33N, A_y = 950\ N, F_{BC} = 3916.67\ N$)



$\xrightarrow{+}$

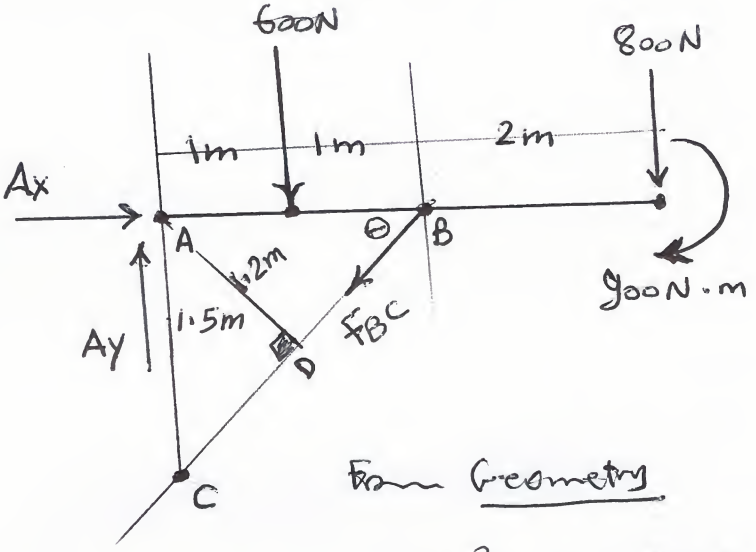
$\Sigma F_x = 0$

$A_x - F_{BC}\cos\theta = 0$

but from Geometry

$\tan\theta = \frac{1.5}{2}$

$A_x = F_{BC}(0.8)$ — (1)



$+\uparrow \Sigma F_y = 0$

$A_y - 600 - F_{BC}\sin\theta - 800 = 0$

$A_y - 1400 - F_{BC}(0.6) = 0$ — (2)

$\overset{+}{\circlearrowleft} \Sigma M_A = 0$

$-600(1) - F_{BC}(1.2) - 800(4) - 900 = 0$

$-4700 - 1.2F_{BC} = 0 \quad \therefore 1.2F_{BC} = -4700$

$F_{BC} = -3916.67\ N$

From Geometry

$\overline{BC}^2 = 4 + 2.25$

$\overline{BC}^2 = 6.25$

$BC = 2.5m$

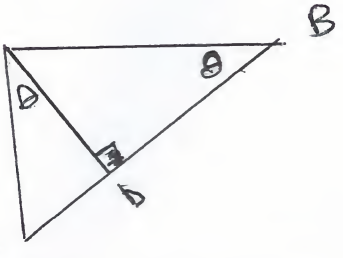
$\sin\theta = \frac{1.5}{2.5} = 0.6$

$\cos\theta = \frac{2}{2.5} = 0.8$

$A_x = 0.8\ F_{BC} = -3133.33\ N$

$A_y = 1400 + 0.6\ F_{BC}$

$A_y = 1400 - 2350 = 950N.$



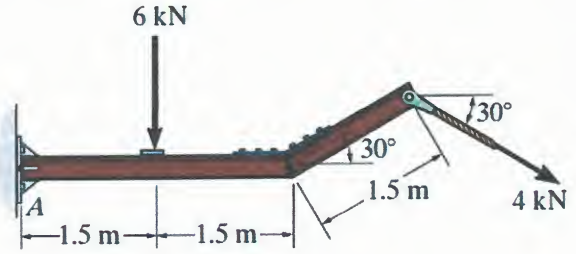
$AD = AB\sin\theta$

$= 2(0.6)$

$= 1.2$

8

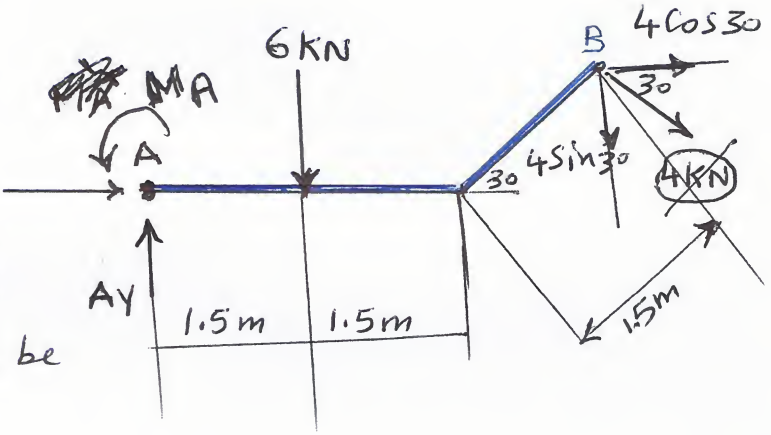
8 Determine the components of the support reactions at the fixed support A on the cantilevered beam.



(Ans. $A_x = 3.46\,kN, A_y = 8\,kN, M_A = 20.2\,kN.m$)

Fixed support at A

we have. A_x, A_y, M_A



$\xrightarrow{+} \Sigma F_x = 0$

$A_x + 4\cos 30 = 0$

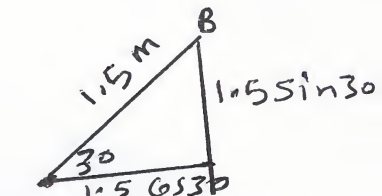
$\therefore A_x = -\frac{4\sqrt{3}}{2} = \boxed{-3.46\ KN}$

$\therefore$ The direction of A_x should be in the -ve x-direction.

$+\uparrow \Sigma F_y = 0$

$A_y - 6 - 4\sin 30 = 0$

$A_y = 6 + 4\left(\frac{1}{2}\right) \quad \therefore \boxed{A_y = 8\ KN}$



From Geometry

to find M_A.

we will take the moment about A:

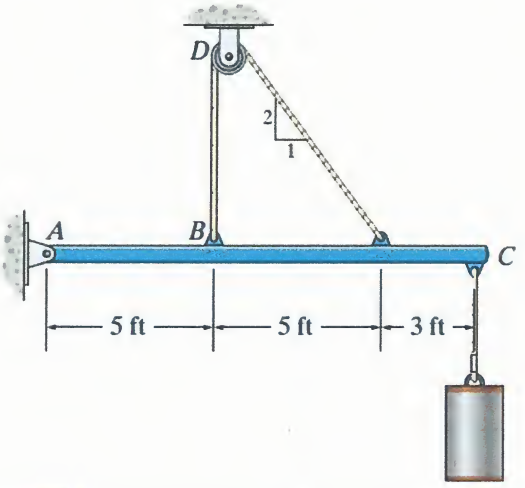
$M_A - 6(1.5) - 4\sin 30\,(1.5\cos 30 + 3) - 4\cos 30\,(1.5\sin 30) = 0$

$M_A - 9 - 8.598 - 2.598 = 0$

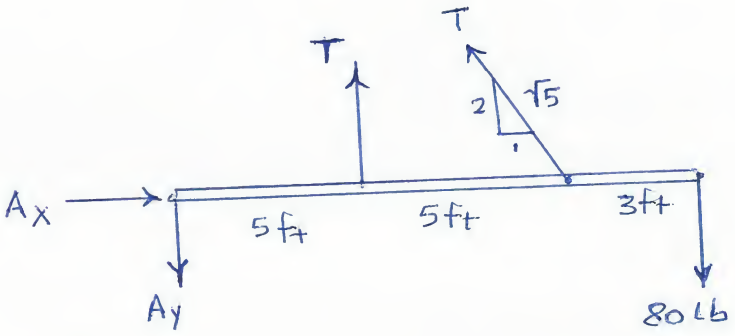
$M_A = 20.2\ KN.m$

9 Determine the tension in the cable and the horizontal and vertical components of reaction of the pin A. The pulley at D is frictionless and the cylinder weighs 80 lb.

(Ans. $A_x = 33.4\ lb,\ A_y = 61.3\ lb, T = 74.6\ lb$)



- Draw Free body diagram.



$\xrightarrow{+} \Sigma F_x = 0$

$A_x - T\left(\frac{1}{\sqrt{5}}\right) = 0$ — (1)

$+\uparrow \Sigma F_y = 0$

$T + T\left(\frac{2}{\sqrt{5}}\right) - 80 - A_y = 0$ — (2)

$\left(\overset{+}{\circlearrowleft}\right) \Sigma M_A = 0$

$T(5) + T\left(\frac{2}{\sqrt{5}}\right)(10) - 80(13) = 0$ — (3)

From (3)

$5T + 8.94T - 1040 = 0$

$13.94T = 1040$

$\therefore \boxed{T = 74.6\ lb}$

From (1)

$A_x = \frac{T}{\sqrt{5}} = 33.4\ lb$

$\boxed{A_x = 33.4\ lb}$

From (2)

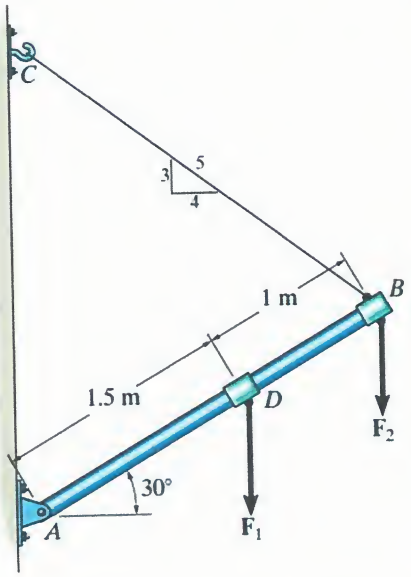
$\boxed{A_y = 61.3\ lb}$

(10)

(10)

10 The boom supports the two vertical loads. Neglect the size of the collars at D and B and the thickness of the boom, and compute the horizontal and vertical components of force at the pin A and the force in cable CB. Set $F_1 = 800\ N$ *and* $F_2 = 350\ N$.

(Ans. $A_x = 625\ N, A_y = 681\ N, F_{CB} = 782\ N$)



$\xrightarrow{+} \Sigma F_x = 0$

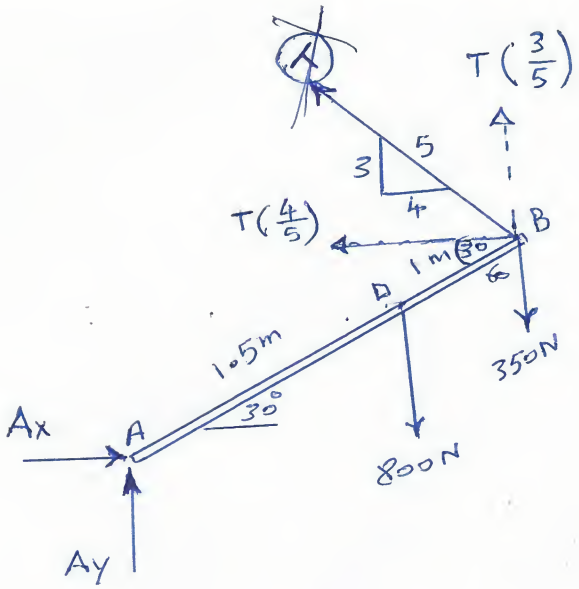
$A_x - T\left(\frac{4}{5}\right) = 0$ — (1)

$+\uparrow \Sigma F_y = 0$

$A_y - 800 - 350 + T\left(\frac{3}{5}\right) = 0$ — (2)

$\left(\Sigma M_A = 0\right)_+$

$-350\,(2.5)(\cos 30) - 800\,(1.5)(\cos 30) + T\left(\frac{4}{5}\right)(2.5 \sin 30) + \left(\frac{3}{5}\right)T\,(2.5 \cos 30) = 0$ — (3)



From (3) we can get T

$-757.772 - 1039.23 + T + 1.299\,T = 0$

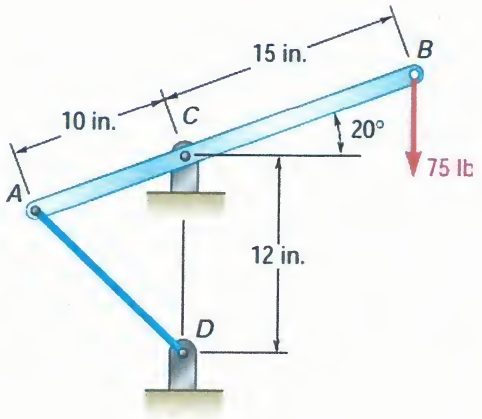
$2.299\,T = 1797$ ∴ $\boxed{T = 782\ N}$

From (1) $A_x = \frac{4}{5}(T) = 625N$ ∴ $\boxed{A_x = 625N}$

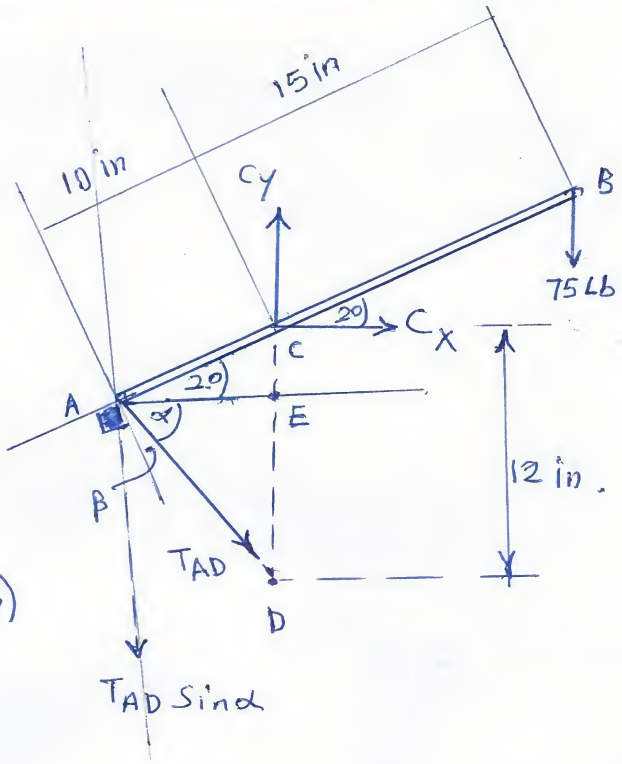
From (3) $A_y - 1150 + \frac{3}{5}(T) = 0$

$\therefore A_y = +1150 - 469.2$ ∴ $\boxed{A_y = 681N}$

11 A lever AB is hinged at C and attached to a control cable at A. If the lever is subjected to a 75-lb vertical force at B, determine (a) the tension in the cable, (b) the reaction at C.



(Ans. $C_x = -88.097\ lb, C_y = 155.435\ lb,\ C = 78.665\ lb,\ T_{AB} = 119.293\ lb$)



$\xrightarrow{+} \Sigma F_x = 0$

$C_x + T_{AD} \cdot \cos\alpha = 0$ — (1)

$+\uparrow \Sigma F_y = 0$

$C_y - 75 - T_{AD} \cdot \sin\alpha = 0$ — (2)

$\overset{+}{\circlearrowleft} \Sigma M_C = 0$

$-75 \times 15(\cos 20) + T_{AD} \sin\alpha \times (10 \cos 20)$

$+ T_{AD} \cos\alpha\ (10 \sin 20)$ — (3)

from (3) if we have α we can get T_{AD}

* From Geometry

$CE = 10 \sin 20 = 3.42$ in.

$AE = 10 \cos 20 = 9.397$ in.

$DE = 12 - CE = 12 - 3.42 = 8.58$ in.

$\therefore \tan\alpha = \frac{DE}{AE} = \frac{8.58}{9.397}$

$\therefore \alpha = \tan^{-1}(0.913)$ $\therefore \boxed{\alpha = 42.396^\circ}$

Problem 11

From ③

$$-1057.154 + 9.397\,T_{AD} * 0.674 + 3.42\,T_{AD} * 0.739 = 0$$

$$6.334\,T_D + 2.527\,T_D = 1057.154$$

$$\therefore T_D = \frac{1057.154}{8.861} = 119.3 \text{ lb}$$

$$\boxed{T_D = 119.3 \text{ lb}}$$

From ①

$$\therefore C_x = -119.3(\cos 42.396) = -88.1 \text{ lb}$$

$$\boxed{C_x = -88.1 \text{ lb}}$$

From ②

$$C_y = 75 + 119.3(\sin 42.396)$$

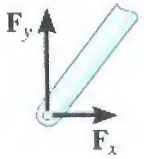
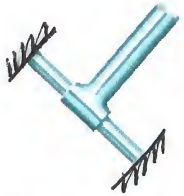
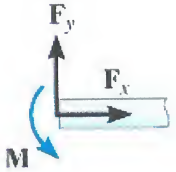
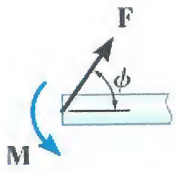
$$\boxed{C_y = 155.438 \text{ lb}}$$

$$C = \sqrt{C_x^2 + C_y^2} = \sqrt{(-88.1)^2 + (155.438)^2} = 178.67 \text{ lb}$$

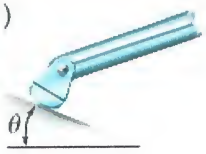
and $\theta = \tan^{-1}\frac{C_y}{C_x} = \frac{155.438}{88.1} = 60.5^\circ$

∴ The resetion of C is 178.67 ∠ 60.5°

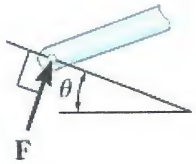
(or) 178.67 lb and angle 119.5 with +ve x-axis.

Types of Connection	Reaction	Number of Unknowns
(8)  smooth pin or hinge	 or 	Two unknowns. The reactions are two components of force, or the magnitude and direction ϕ of the resultant force. Note that ϕ and θ are not necessarily equal [usually not, unless the rod shown is a link as in (2)].
(9)  member fixed connected to collar on smooth rod		Two unknowns. The reactions are the couple moment and the force which acts perpendicular to the rod.
(10)  fixed support	 or 	Three unknowns. The reactions are the couple moment and the two force components, or the couple moment and the magnitude and direction ϕ of the resultant force.

(5)

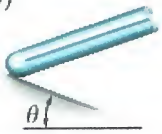


rocker

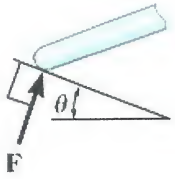


One unknown. The reaction is a force which acts perpendicular to the surface at the point of contact.

(6)

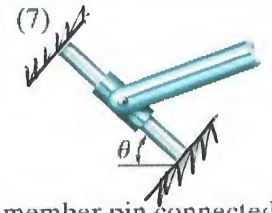


smooth contacting surface

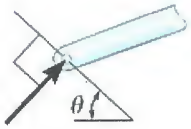


One unknown. The reaction is a force which acts perpendicular to the surface at the point of contact.

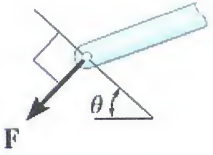
(7)



member pin connected to collar on smooth rod



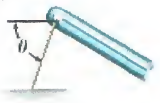
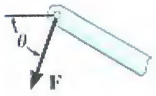
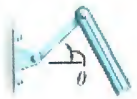
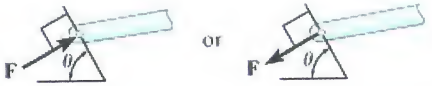
or



One unknown. The reaction is a force which acts perpendicular to the rod.

continued

TABLE 5–1 Supports for Rigid Bodies Subjected to Two-Dimensional Force Systems

Types of Connection	Reaction	Number of Unknowns
(1)  cable		One unknown. The reaction is a tension force which acts away from the member in the direction of the cable.
(2)  weightless link		One unknown. The reaction is a force which acts along the axis of the link.
(3)  roller		One unknown. The reaction is a force which acts perpendicular to the surface at the point of contact.
(4)  roller or pin in confined smooth slot		One unknown. The reaction is a force which acts perpendicular to the slot.